## Optimisation and control of synchrotron emission in ultra-intense laser-solid interactions using machine learning - Supplementary material

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## 1. Acceptance function

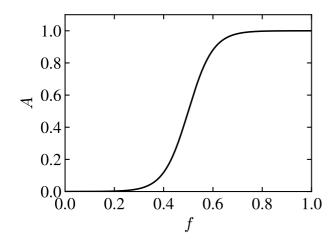


Figure 1 : The acceptance function used in the objective function  $f_{M2}$  for Bayesian optimisation, with  $f_{max}=1$ .

The acceptance function  $A\left(f\right)=1/(1+\exp(-(20/f_{max})(f-0.5f_{max})))$  described in section 4 of the main text is shown in figure 1, where  $f_{max}=1$  is arbitrarily chosen.

## 2. Spatial profiles of synchrotron emission for $I_l=3\times 10^{23}\,{ m W\,cm^{-2}}$ in 3D

The angle-resolved total energy of synchrotron emission,  $d\sum \varepsilon_{sy}/d\Omega$ , is shown in figures 2, 3 and 4 for p-, s- and left-hand c-polarisation, respectively, for 3D simulations of the interaction with peak laser intensity  $I_L=3\times 10^{23}\,\mathrm{W\,cm^{-2}}$ , as described in the main text. Results for target thicknesses of  $l=1\,\mu\mathrm{m}$  and  $3\,\mu\mathrm{m}$  are shown for laser pulse angle-of-incidence values of  $\theta_i=0,45^\circ$  and  $67.5^\circ$ .

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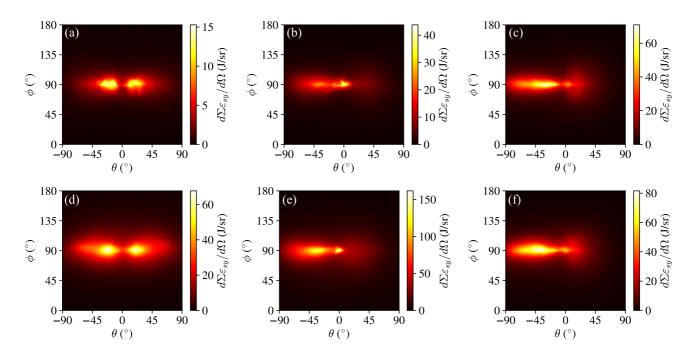


Figure 2: Angle-resolved total energy of synchrotron emission for a p-polarised laser pulse, for (a)–(c)  $1 \mu$ m target thickness and (d)–(f)  $3 \mu$ m target thickness. The angle-of-incidence is (a) and (d)  $0^{\circ}$ , (b) and (e)  $45^{\circ}$ , (c) and (c)  $67.5^{\circ}$ .

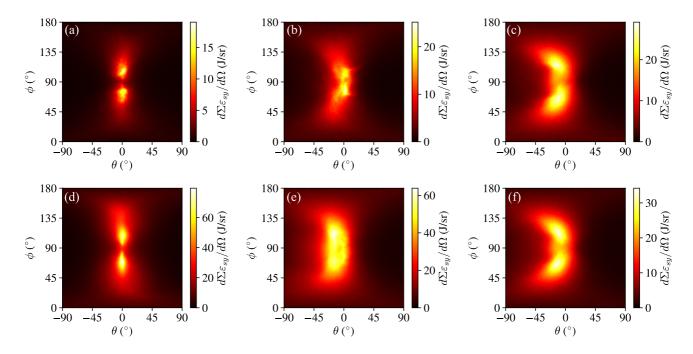


Figure 3: Angle-resolved total energy of synchrotron emission for an s-polarised laser pulse, for (a)–(c) 1  $\mu$ m target thickness and (d)–(f) 3  $\mu$ m target thickness. The angle-of-incidence is (a) and (d) 0°, (b) and (e) 45°, (c) and (c) 67.5°.

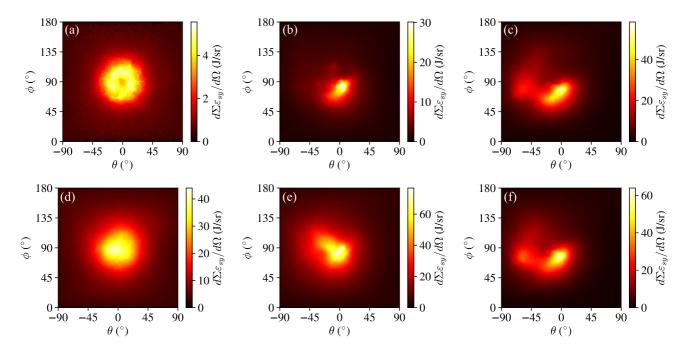


Figure 4: Angle-resolved total energy of synchrotron emission for a left-hand c-polarised laser pulse, for (a)–(c) 1  $\mu$ m target thickness and (d)–(f) 3  $\mu$ m target thickness. The angle-of-incidence is (a) and (d) 0°, (b) and (e) 45°, (c) and (c) 67.5°...