Supplementary material

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Figure S1: Alignment of the focal series for reconstruction using the simultaneously acquired ADF-STEM images. The positions of the atom columns are determined by 2D Gaussian fitting using the Atomap package [8]. The rectangular grid implied by these atom positions (plotted with the unbroken coloured lines) is then smoothly deformed to match a perfect square grid (plotted with the dotted colored line) to correct the probe positions \mathbf{R} that form part of the input to the reconstruction algorithm (Algorithm 1 in the main text).



Figure S2: Estimation of the defocus correction using the geometric blur of images of gold nanoparticles on an amorphous carbon film. For each of the images in an ADF-STEM focal series we convolve the image identified as being "in-focus" with a top-hat function with radius $\Delta f \tan \alpha$, as indicated by the diagram inset, where α is the probe forming aperture in radians (20 mrad for this experiment) and the value of Δf is optimized to minimize the least squares difference between the convolved in-focus image and the experimental result for each image in the series to estimate the true defocus. Plotted above is the nominal defocus read from the microscope software against the defocus estimated via the minimization process. A trendline with slope 1.24 is fitted to the datapoints meaning that software defocus values must be corrected with a multiplicative factor of 1.24. The in-focus image and two experimental images (labelled Exp) with the most extreme defocus values alongside the blurred in-focus image (labelled Blurred) are shown for reference.



Figure S3: Convergence of the error metric $\varepsilon = \frac{\sum |\sqrt{I(\Delta.f,\mathbf{R},\mathbf{k})} - |\sum_{\mathbf{h}} S^{0}_{\mathbf{r},\mathbf{h}}\psi_{\mathbf{h}}(\Delta.f,\mathbf{R})||^{2}}{\sum |I(\Delta f,\mathbf{R},\mathbf{k})|^{2}}$ for the *S*-matrix reconstruction for the PIO-YSZ dataset with iteration number of the algorithm described in the main manuscript.



Figure S4: Reconstructed components of the S-matrix reconstruction for the PIO-YSZ sample from Fig. 2 of the main manuscript.



Figure S5: Mutlislice ptychography reconstructions from all 4D-STEM datasets.

Density functional theory calculation details

To account for the alternating pattern of oxygen columns lacking in STEM reconstructions, we considered the atomic-scale disorder that could occur in an epitaxial thin film sample with ion milling or electron beam damage sustained during preparation and imaging. Density functional theory (DFT) was used to determine the extent of such compositional and structural influences on oxygen positions within the pyrochlore structure. This was quantified by the oxygen positional parameter x (see main text) where x=0.3125 gives maximum off-centering and x=0.375 gives a centered oxygen column. The calculated stoichiometric bulk structure has x=0.330 which indicates a significant amount of splaying that can be discerned in the alternating pattern of oxygen columns in the STEM simulations. The results in Table 1 in the main text were extracted from DFT-optimized structures with the following modifications.

Firstly, we consider the effect of the epitaxial YSZ interface on the Pb₂Ir₂O₇ structure. The lattice parameter of YSZ (10.28 Å) is equivalent to a small (0.45%) tensile strain on the calculated Pb₂Ir₂O₇ lattice parameter; enforcing this strain in-plane in a geometry optimization resulted in x=0.332. The measured in-plane lattice parameter for PIO on YSZ was 10.248 Å, indicating that an even smaller amount of tensile strain may be present in the PIO layer, with negligible change in x, thus biaxial strain alone cannot account for the areas observed with centering on all oxygen columns. Further considering the PIO(001)/YSZ(001) explicitly in supercell calculations gave no indication that the YSZ structure altered the oxygen positions in Pb₂Ir₂O₇.

Secondly, we consider the effect of cation antisite defects. The ratio of cation radii is large $(r_{Pb2+}/r_{Ir4+} = 2.06)$ compared to other pyrochlores where cation site disorder is common [7], therefore few cation antisite defects are expected. We create antisite defects in the structure by switching Ir and Pb positions, where one swap creates 2 antisite defects. In the 88 atom unit cell, an Ir on a Pb site contributes 1/16 toward the the total cation side disorder, and similarly for a Pb on an Ir site, therefore one swap results in 12.5% total amount of antisite defects. Including 12.5%, 25%, 37% and 50% of antisite defects resulted in an increase in x to average values 0.336, 0.337, 0.344 and 0.342 respectively. This indicates that a large proportion of antisite defects could induce a structural change noticeable in STEM. Simulated STEM images of these concentrations of defects are shown in Fig. S5, in which the defects disorder the oxygen columns to some degree, though a satisfactory match with experiment is not achieved even at the highest defect concentration.

Finally, we consider the influence of oxygen vacancies, which are expected to be present in significant concentrations. With O-vacancies in the preferred position in PbO₄ tetrahedra [10], we optimized the pyrochlore with Pb₂Ir₂O_{6.5} and Pb₂Ir₂O₆ stoichiometries. We find that the *x* parameter changes negligibly when O-vacancies are included: Pb₂Ir₂O_{6.5} x=0.327-0.329, and Pb₂Ir₂O₆ x=0.327, which translates to a maximum shift of the O positions of 0.03 Å - indicating that the pyrochlore structure is extremely tolerant to oxygen vacancies. To be sure that the mixed valence of Ir in Pb₂Ir₂O_{6.5} is captured in calculations (50% Ir⁴⁺, 50% Ir⁵⁺), due to the known shortcomings of standard (semilocal) DFT in describing electron localization, we also considered these structures with a higher level of theory - hybrid DFT - which again resulted in a negligible change in the oxygen columns (x=0.328-0.331).

In summary, none of the considered structural variations - biaxial strain, cation antisites and oxygen vacancies - could account for the regions of tighter oxygen columns. The perovskite phase, which has aligned O-columns inherent to the structure, is also unlikely due to the large energy difference compared to the pyrochlore ($\Delta E_{pyro-perov} = -1.1 \text{ eV}$) and the large strain (9%). Instead, these regions may be the result of larger compositional variations or nanodomains as summarized in the main text.

DFT Methods: Geometry optimizations were performed using DFT with the Vienna *Ab initio* Simulation Package VASP [2, 3, 4, 5], using projector augmented wave (PAW) pseudopotentials [1, 6] including Pb 5*d* 6*sp*, Ir 5*spd*, 6*s*, O 2*s* 2*p* electrons as valence. We used the PBEsol exchange-correlation functional [9] and a U value of 1.69 eV applied to the Ir 5*d* orbitals to account for localization. We found an energy cutoff of 700 eV and Γ -centered k-point grid $4 \times 4 \times 4$ converged energies to 1 meV per atom. The self-consistent field energy was converged to 10^{-7} eV and forces were converged to 1 meVÅ⁻¹. This gave a calculated lattice constant of 10.234 Å for Pb₂Ir₂O₇. For verifying structures containing mixed valence cations, the HSEsol functional was used [11].

References

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