

$$T_{\text{RMA,sky}}^p = T_{\text{sky}} + \Delta T_{\text{TL}}^p \quad (1)$$

$$\Delta T_{\text{TL}}^p = (1 - t_{\text{TL}}^p)(T_{\text{air}} - T_{\text{sky}}) \quad (2)$$

$$t_{\text{TL}}^p = 10^{-L_{\text{TL}}^p/10} \quad (3)$$

$$T_{\text{source}}^{p,ch}(T_{\text{CA}}) = \frac{T_{\text{RS}} - T_{\text{RMA,sky}}^p}{U_{\text{RS}}^{ch} - U_{\text{sky}}^{p,ch}} (U_{\text{source}}^{ch} - U_{\text{sky}}^{p,ch}) + T_{\text{RMA,sky}}^p \quad \text{for } source = \{\text{ACS, HS}\} \quad (4)$$

$$T_{\text{ACS}}(T_{\text{CA}}) = 26.7715 + 0.2474 \cdot T_{\text{CA}} \quad (5)$$

$$T_{\text{HS}}(T_{\text{CA}}) = 633.5730 + 0.8175 \cdot T_{\text{CA}} \quad (6)$$

$$T_{\text{A}}^{p,ch} = \frac{T_{\text{HS}}(T_{\text{CA}}) - T_{\text{ACS}}(T_{\text{CA}})}{U_{\text{HS}}^{ch} - U_{\text{ACS}}^{ch}} \cdot (U_{\text{RMA}}^{p,ch} - U_{\text{ACS}}^{ch}) + T_{\text{ACS}}(T_{\text{CA}}) \quad (7)$$

$$\Delta T_{\text{A}}^{p,ch}(\theta_{\text{A}}) = \sqrt{\Delta T_{\text{RFI}}^{p,ch}(\theta_{\text{A}})^2 + \Delta T_{\text{RS}}^{ch^2} + \Delta T_{\text{ELBARA-III}}^2} \quad (8)$$

$$CF(W_{\text{S}}, \rho_{\text{S}}) = \sum_{\theta_{\text{A}}, p} \frac{(T_{\text{A}}^p(\theta_{\text{A}}) - T_{\text{A, sim}}^p(\theta_{\text{A}}, W_{\text{S}}, \rho_{\text{S}}))^2}{\Delta T_{\text{A}}^p(\theta_{\text{A}})^2} \quad (9)$$

$$\begin{cases} T_{\text{A}}^{\text{H}}(\theta_{\text{A}}) = T_{\text{A, sim}}^{\text{H}}(\theta_{\text{A}}, W_{\text{S}}^{\theta_{\text{A}}}, \rho_{\text{S}}^{\theta_{\text{A}}}) \\ T_{\text{A}}^{\text{V}}(\theta_{\text{A}}) = T_{\text{A, sim}}^{\text{V}}(\theta_{\text{A}}, W_{\text{S}}^{\theta_{\text{A}}}, \rho_{\text{S}}^{\theta_{\text{A}}}) \end{cases} \quad (10)$$

$$\hat{\mathbf{K}}_{\text{F}}(\theta_{\text{F}}, \varphi_{\text{F}}) = \begin{pmatrix} \sin\theta_{\text{F}} \cdot \sin\varphi_{\text{F}} \\ \sin\theta_{\text{F}} \cdot \cos\varphi_{\text{F}} \\ -\cos\theta_{\text{F}} \end{pmatrix} \quad (11)$$

$$\widehat{\mathbf{H}}_{\mathbf{F}}(\theta_{\mathbf{F}}, \varphi_{\mathbf{F}}) = \frac{\widehat{\mathbf{K}}_{\mathbf{F}} \otimes \widehat{\mathbf{Z}}}{|\widehat{\mathbf{K}}_{\mathbf{F}} \otimes \widehat{\mathbf{Z}}|} = \frac{1}{N_{\mathbf{H},\mathbf{F}}} \begin{pmatrix} \sin\theta_{\mathbf{F}} \cdot \cos\varphi_{\mathbf{F}} \\ -\sin\theta_{\mathbf{F}} \cdot \sin\varphi_{\mathbf{F}} \\ 0 \end{pmatrix} \text{ with normalization} \quad (12)$$

$$N_{\mathbf{H},\mathbf{F}} = |\sin\theta_{\mathbf{F}}|$$

$$\widehat{\mathbf{V}}_{\mathbf{F}}(\theta_{\mathbf{F}}, \varphi_{\mathbf{F}}) = \frac{\widehat{\mathbf{K}}_{\mathbf{F}} \otimes \widehat{\mathbf{H}}_{\mathbf{F}}}{|\widehat{\mathbf{K}}_{\mathbf{F}} \otimes \widehat{\mathbf{H}}_{\mathbf{F}}|} = \frac{1}{N_{\mathbf{V},\mathbf{F}}} \begin{pmatrix} -\cos\theta_{\mathbf{F}} \cdot \sin\theta_{\mathbf{F}} \cdot \sin\varphi_{\mathbf{F}} \\ -\cos\theta_{\mathbf{F}} \cdot \sin\theta_{\mathbf{F}} \cdot \cos\varphi_{\mathbf{F}} \\ -\sin^2\theta_{\mathbf{F}} \end{pmatrix} \text{ with normalization} \quad (13)$$

$$N_{\mathbf{V},\mathbf{F}} = \sqrt{(\cos\theta_{\mathbf{F}} \cdot \sin\theta_{\mathbf{F}} \cdot \sin\varphi_{\mathbf{F}})^2 + (\cos\theta_{\mathbf{F}} \cdot \sin\theta_{\mathbf{F}} \cdot \cos\varphi_{\mathbf{F}})^2 + \sin^4\theta_{\mathbf{F}}}$$

$$\widehat{\mathbf{K}}_{\mathbf{A}}(\theta_{\mathbf{A}}) = \begin{pmatrix} 0 \\ \sin\theta_{\mathbf{A}} \\ -\cos\theta_{\mathbf{A}} \end{pmatrix} \quad (14)$$

$$\widehat{\mathbf{H}}_{\mathbf{A}}(\theta_{\mathbf{A}}) = \frac{1}{N_{\mathbf{A},\mathbf{H}}} \begin{pmatrix} \sin\theta_{\mathbf{A}} \\ 0 \\ 0 \end{pmatrix} \text{ with normalization} \quad (15)$$

$$N_{\mathbf{A},\mathbf{H}} = \sin\theta_{\mathbf{A}}$$

$$\widehat{\mathbf{V}}_{\mathbf{A}}(\theta_{\mathbf{A}}) = \frac{1}{N_{\mathbf{A},\mathbf{V}}} \begin{pmatrix} 0 \\ -\cos\theta_{\mathbf{A}} \cdot \sin\theta_{\mathbf{A}} \\ -\sin^2\theta_{\mathbf{A}} \end{pmatrix} \text{ with normalization} \quad (16)$$

$$N_{\mathbf{A},\mathbf{V}} = \sqrt{(\cos\theta_{\mathbf{A}} \cdot \sin\theta_{\mathbf{A}})^2 + \sin^4\theta_{\mathbf{A}}}$$

$$H_{\mathbf{A}}^{\mathbf{H}\mathbf{F}} = \widehat{\mathbf{H}}_{\mathbf{F}} \odot \widehat{\mathbf{H}}_{\mathbf{A}} = \cos\varphi_{\mathbf{F}} \quad (17)$$

$$H_{\mathbf{A}}^{\mathbf{V}\mathbf{F}} = \widehat{\mathbf{V}}_{\mathbf{F}} \odot \widehat{\mathbf{H}}_{\mathbf{A}} = \cos\theta_{\mathbf{F}} \cdot \sin\varphi_{\mathbf{F}} \quad (18)$$

$$V_{\mathbf{A}}^{\mathbf{V}\mathbf{F}} = \widehat{\mathbf{V}}_{\mathbf{F}} \odot \widehat{\mathbf{V}}_{\mathbf{A}} = \cos\varphi_{\mathbf{F}} \cdot \cos\theta_{\mathbf{A}} \cdot \cos\theta_{\mathbf{F}} + \sin\theta_{\mathbf{A}} \cdot \sin\theta_{\mathbf{F}} \quad (19)$$

$$V_{\mathbf{A}}^{\mathbf{H}\mathbf{F}} = \widehat{\mathbf{H}}_{\mathbf{F}} \odot \widehat{\mathbf{V}}_{\mathbf{A}} = \cos\theta_{\mathbf{A}} \cdot \sin\varphi_{\mathbf{F}} \quad (20)$$

$$\mathbf{E}_A^H = \begin{pmatrix} H_A^{HF} \cdot E_F^H \\ H_A^{VF} \cdot E_F^V \end{pmatrix} \quad \text{and} \quad \mathbf{E}_A^V = \begin{pmatrix} V_A^{HF} \cdot E_F^H \\ V_A^{VF} \cdot E_F^V \end{pmatrix} \quad (21)$$

$$T_{A,F}^H \propto |\mathbf{E}_A^H|^2 = H_A^{HF^2} \cdot T_F^H + H_A^{VF^2} \cdot T_F^V \quad \text{and} \quad T_{A,F}^V \propto |\mathbf{E}_A^V|^2 = V_A^{HF^2} \cdot T_F^H + V_A^{VF^2} \cdot T_F^V \quad (22)$$

$$T_A^H = \frac{1}{N} \iint_{\Omega} T_{A,F}^H \cdot D \cdot d\Omega = \frac{1}{N} \int_{\theta_F} \int_{\varphi_F} \left(H_A^{HF^2} \cdot T_{B,F}^H + H_A^{VF^2} \cdot T_{B,F}^V \right) \cdot D \cdot \sin\theta_F \cdot d\theta_F \cdot d\varphi_F \quad (23)$$

$$T_A^V = \frac{1}{N} \iint_{\Omega} T_{A,F}^V \cdot D \cdot d\Omega = \frac{1}{N} \int_{\theta_F} \int_{\varphi_F} \left(V_A^{HF^2} \cdot T_{B,F}^H + V_A^{VF^2} \cdot T_{B,F}^V \right) \cdot D \cdot \sin\theta_F \cdot d\theta_F \cdot d\varphi_F \quad (24)$$

$$D(\alpha) = \exp[-\alpha^2/\alpha_0^2] \quad \text{with} \quad \alpha_0 = 13.8366^\circ \quad (25)$$

$$\cos\alpha = \hat{\mathbf{R}}_F \odot \hat{\mathbf{R}}_A = \cos\theta_A \cdot \cos\theta_F + \cos\varphi_F \cdot \sin\theta_A \cdot \sin\theta_F \quad (26)$$

$$N = \iint_{\Omega} D \cdot d\Omega = \int_{\theta_F} \int_{\varphi_F} D \cdot \sin\theta_F \cdot d\theta_F \cdot d\varphi_F \quad (27)$$

$$T_F^p(\theta_F) = \begin{cases} T_{LS-MEMLS}^p(\theta_F) & \text{for: } 0^\circ \leq \theta_F \leq 90^\circ \quad (\text{below horizon}) \\ T_{sky}(180^\circ - \theta_F) & \text{for: } 90^\circ < \theta_F \leq 180^\circ \quad (\text{above horizon}) \end{cases} \quad (28)$$