

# Turbulent Rayleigh-Bénard convection in a strong vertical magnetic field

(supplemental materials)

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This document summarizes the results of sections 2.4 *Grid sensitivity study* and 3.2 *Global transport properties* in the main article.

## 1. Grid sensitivity study

The results of the grid sensitivity study are presented in table below. The number of grid points inside the smallest thickness, which is  $\delta_v$  for the cases with  $Ha = 0$  and  $\delta_{Ha}$  for the cases with  $Ha > 0$  is shown as  $N_{BL}$ . Other definitions of the listed quantities can be found in the main article.

<i>Run</i>	<i>Ra</i>	<i>Ha</i>	$N_r \times N_z \times N_\theta$	$A_z$	$N_{BL}$	$Nu$	$Re$
1	$10^7$	0	$128 \times 128 \times 128$	3.0	8	10.52	7179
2	$10^7$	0	$192 \times 192 \times 192$	3.0	12	10.31	7075
3	$10^8$	0	$192 \times 192 \times 192$	3.0	8	19.68	20428
4	$10^8$	0	$256 \times 256 \times 256$	3.0	11	19.51	20408
5	$10^9$	0	$192 \times 192 \times 192$	3.0	5	40.47	59689
6	$10^9$	0	$256 \times 256 \times 256$	3.0	7	40.57	63434
7	$10^9$	0	$384 \times 384 \times 384$	3.0	11	40.85	58239
8	$10^7$	450	$192 \times 64 \times 192$	4.0	8	5.16	2513
9	$10^7$	450	$192 \times 96 \times 192$	3.5	8	5.43	2281
10	$10^7$	450	$192 \times 192 \times 192$	3.0	7	5.35	2202
11	$10^7$	650	$192 \times 64 \times 192$	4.0	6	3.86	1616
12	$10^7$	650	$192 \times 96 \times 192$	3.5	6	3.84	1690
13	$10^7$	650	$192 \times 192 \times 192$	3.0	7	3.63	1638
14	$10^8$	650	$192 \times 96 \times 192$	3.5	6	13.19	8366
15	$10^8$	650	$192 \times 192 \times 192$	3.0	7	12.76	8369
16	$10^8$	650	$256 \times 256 \times 256$	3.0	10	13.32	8311
17	$10^8$	850	$192 \times 64 \times 192$	4.0	6	10.76	7326
18	$10^8$	850	$192 \times 192 \times 192$	3.0	6	10.62	7476
19	$10^8$	850	$256 \times 256 \times 256$	3.0	7	10.65	6842
20	$10^9$	850	$192 \times 96 \times 192$	4.0	9	33.67	28204
21	$10^9$	850	$192 \times 192 \times 192$	3.0	6	32.60	24971
22	$10^9$	850	$256 \times 256 \times 256$	3.0	7	31.92	25239
23	$10^9$	1400	$192 \times 96 \times 192$	4.0	6	26.37	23348
24	$10^9$	1400	$192 \times 192 \times 192$	3.0	4	25.78	21034
25	$10^9$	1400	$256 \times 256 \times 256$	3.0	5	25.85	22547

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Although the comparison between the maximum grid step in the bulk with the estimates of the Kolmogorov length scale indicate that the non-magnetic flow at  $Ra = 10^9$  is somewhat under-resolved, as already mentioned in the main article, the data convincingly shows that the regimes of the focus of this study (high  $Ra$  and  $Ha$ ) are well-resolved.

## 2. Global transport properties

For each combination of  $Ha$  and  $Ra$ , the tables show the Nusselt  $Nu$  and Reynolds  $Re$  numbers, as well as the thickness of the thermal boundary layer  $\delta_T$  defined in the main article. For the latter, the computed value  $\delta_T^{DNS}$  and the theoretical value  $\delta_T \approx 1/(2Nu)$  are listed.

$Ha$	$Ra$	$Nu$	$Re$	$\delta_T \times 10^2$	$\delta_T^{DNS} \times 10^2$
1400	$7 \times 10^7$	5.60	4066	8.921	8.950
1400	$9 \times 10^7$	6.58	5022	7.593	7.743
1400	$10^8$	6.97	5190	7.172	7.182
1400	$3 \times 10^8$	13.36	10402	3.742	3.749
1400	$5 \times 10^8$	17.49	15886	2.858	2.883
1400	$7 \times 10^8$	21.89	17892	2.284	2.301
1400	$9 \times 10^8$	24.86	19256	2.011	2.008
1400	$10^9$	25.85	22547	1.934	1.949

$Ha$	$Ra$	$Nu$	$Re$	$\delta_T \times 10^2$	$\delta_T^{DNS} \times 10^2$
850	$10^7$	2.93	1429	17.090	17.119
850	$3 \times 10^7$	5.41	3188	9.242	9.272
850	$5 \times 10^7$	7.39	4507	6.770	6.773
850	$7 \times 10^7$	8.84	5240	5.654	5.645
850	$9 \times 10^7$	10.30	6634	4.855	4.830
850	$10^8$	10.65	6842	4.695	4.724
850	$3 \times 10^8$	18.78	13734	2.662	2.676
850	$5 \times 10^8$	23.77	17749	2.103	2.118
850	$7 \times 10^8$	27.26	21971	1.834	1.843
850	$9 \times 10^8$	30.79	24724	1.624	1.632
850	$10^9$	31.92	25239	1.566	1.563

$Ha$	$Ra$	$Nu$	$Re$	$\delta_T \times 10^2$	$\delta_T^{DNS} \times 10^2$
650	$10^7$	3.84	1632	13.026	13.126
650	$3 \times 10^7$	6.77	3805	7.389	7.439
650	$5 \times 10^7$	9.06	5233	5.521	5.526
650	$7 \times 10^7$	10.47	5946	4.776	4.812
650	$9 \times 10^7$	11.84	7790	4.222	4.237
650	$10^8$	12.59	8549	3.971	4.001
650	$3 \times 10^8$	21.31	14844	2.346	2.357
650	$5 \times 10^8$	26.29	18958	1.902	1.925
650	$7 \times 10^8$	30.48	23278	1.640	1.661
650	$9 \times 10^8$	33.76	25829	1.481	1.498
650	$10^9$	35.15	27810	1.423	1.444

$Ha$	$Ra$	$Nu$	$Re$	$\delta_T \times 10^2$	$\delta_T^{DNS} \times 10^2$
450	$10^7$	5.24	2234	9.548	9.610
450	$3 \times 10^7$	8.64	4583	5.785	5.801
450	$5 \times 10^7$	11.04	6480	4.528	4.531
450	$7 \times 10^7$	12.95	8100	3.862	3.898
450	$9 \times 10^7$	14.94	8911	3.346	3.363
450	$10^8$	14.98	9711	3.337	3.326
450	$3 \times 10^8$	23.88	18686	2.094	2.108
450	$5 \times 10^8$	28.98	24096	1.725	1.745
450	$7 \times 10^8$	32.88	29430	1.520	1.546
450	$9 \times 10^8$	35.59	33187	1.405	1.439
450	$10^9$	36.98	33753	1.352	1.379

$Ha$	$Ra$	$Nu$	$Re$	$\delta_T \times 10^2$	$\delta_T^{DNS} \times 10^2$
0	$10^7$	10.31	7075	4.848	4.848
0	$3 \times 10^7$	13.68	11929	3.655	3.650
0	$5 \times 10^7$	16.09	13637	3.107	3.118
0	$7 \times 10^7$	17.97	16768	2.783	2.785
0	$9 \times 10^7$	18.67	19239	2.677	2.684
0	$10^8$	19.51	20408	2.562	2.547
0	$3 \times 10^8$	27.16	34055	1.841	1.845
0	$5 \times 10^8$	31.48	42203	1.588	1.588
0	$7 \times 10^8$	34.94	47814	1.431	1.439
0	$9 \times 10^8$	38.80	54015	1.289	1.295
0	$10^9$	40.85	58239	1.224	1.235