## Supplementary Material C. Wave characteristics and parameter variation

Here we present how the wave properties vary for the different studies presented in §§4.1-4.4, in particular as the pycnocline thickness  $\delta$  is varied. The incident wave amplitude a, wavelength  $\lambda$  and wave speed  $c_x$  are presented in figure S2. Black markers are used for the varying  $\delta$  study (§4.1), a yellow to red color map for the varying energy study (§4.2) in figure S2(a-c), and a green to blue colormap for the varying  $\Delta \rho$  study (§4.3) in figure S2(d-e). The changes in the topographic slope do not impact the values considered here.

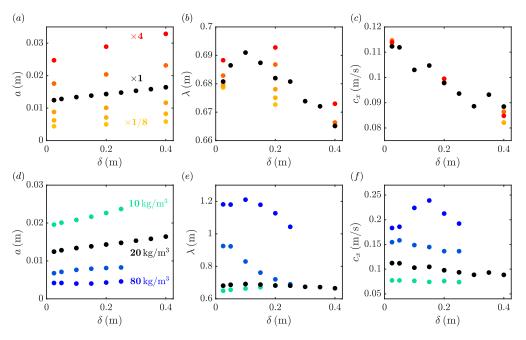


Figure S2: Amplitude a, wavelength  $\lambda$  and propagation speed  $c_x$  of the incident wave, as a function of  $\delta$ , for (a-c) variable  $E_k/E_{k,0}$ , energy grows from yellow to red, (d-f) variable  $\Delta \rho$ , density change grows from green to blue. Black markers represent the pycnocline thickness variation study, with  $E_k/E_{k,0} = 1$  and  $\Delta \rho = 20 \,\mathrm{kg/m^3}$ .