

Supplementary Material for “Stability analysis of a particle  
band on the fluid fluid interface”

### Full Expression for Growth Matrix

The expressions for each component of the  $2 \times 2$  growth matrix,  $G_{jk,n}$ , in Eq. (3.11) of the manuscript are as follows:

$$G_{11} = \frac{6\beta Q (\mu_1 - \mu_2) (E_{22}\bar{R}_1^{n-2} - E_{21}\bar{R}_1^{-(n+2)})}{\pi b^3 (E_{11}E_{22} - E_{12}E_{21})} - \frac{Q}{2\pi b\bar{R}_1^2} \left( 1 + \frac{\phi_2 - \phi_0}{\phi_2 - \frac{\phi_0}{\beta}} \right), \quad (\text{S1a})$$

$$G_{12} = \frac{\beta (E_{11}\bar{R}_1^{-(n+1)} - E_{12}\bar{R}_1^{n-1})}{E_{11}E_{22} - E_{12}E_{21}} \left[ \frac{\gamma(n-1)}{\bar{R}_2^2} - \frac{6\mu_2 Q}{\pi b^3 \bar{R}_2} \right], \quad (\text{S1b})$$

$$G_{21} = \frac{6Q (\mu_1 - \mu_2) (E_{22}\bar{R}_2^{n-1} - E_{21}\bar{R}_2^{-(n+1)})}{\pi b^3 \bar{R}_1 (E_{11}E_{22} - E_{12}E_{21})}, \quad (\text{S1c})$$

$$G_{22} = \frac{(E_{11}\bar{R}_2^{-(n+1)} - E_{12}\bar{R}_2^{n-1})}{E_{11}E_{22} - E_{12}E_{21}} \left[ \frac{\gamma(n-1)}{\bar{R}_2^2} - \frac{6\mu_2 Q}{\pi b^3 \bar{R}_2} \right] - \frac{Q}{2\pi b\bar{R}_2^2}, \quad (\text{S1d})$$

where

$$E_{11} = 12 \left( \frac{\mu_1 - \mu_2}{b^2 n} \right) \bar{R}_1^n + 2(\mu_2 - \mu_1)(n-1)\bar{R}_1^{n-2}, \quad (\text{S1e})$$

$$E_{12} = 12 \left( \frac{\mu_1 + \mu_2}{b^2 n} \right) \bar{R}_1^{-n} - 2(\mu_1 + \mu_2)(n+1)\bar{R}_1^{-(n+2)}, \quad (\text{S1f})$$

$$E_{21} = \left( \frac{-12\mu_2}{b^2 n} \right) \bar{R}_2^n + 2\mu_2(n-1)\bar{R}_2^{n-2}, \quad (\text{S1g})$$

$$E_{22} = \left( \frac{12\mu_2}{b^2 n} \right) \overline{R}_2^{-n} - 2\mu_2 (n+1) \overline{R}_2^{-(n+2)}. \quad (\text{S1h})$$