Supplemental Text 1: Code for Determining Minimum Sample Size

#Install packages and load libraries

install.packages("Bchron")

library("Bchron")

setwd("D:/Folder")

#Define sample space

#Oldest atlatl calendar date (CYBP) [USER ADDED VALUE]

OldAtlDate <- 9539

#Timing of transition (CYBP) [USER ADDED VALUE]

TransDateSampUn <- 1114

#Youngest bow calendar date (CYBP) [USER ADDED VALUE]

YoungBowDate <- 0

#Radiocarbon Date Standard Error [USER ADDED VALUE]

StandardRadError <- 50

#Prior Ranges (CYBP)

AtlRange <- c(OldAtlDate:TransDateSampUn)

BowRange <- c(TransDateSampUn:YoungBowDate)

#Sample sizes:

#Add sample size iterator here [USER ADDED VALUE]

g <- 100

# Interval to iterate through the sequence of sample sizes [USER ADDED VALUE]

j <- 1

#Iterate through error calculation h times for sample size = {1, 2, 3, ..., g}

#Number of times to repeat error stat calculations [USER ADDED VALUE]

h <- 1000

RepVec <- 1:h

#Create an empty vector to store overlapping error values throughout iterations

Overlap.h.Iterations <- rep(NA, h)

#Create empty matrix to store sample size, standard deviation (RMSE), and mean absolute error (MAE)

Stat.matrix <- matrix(nrow = g/j, ncol = 6)

Col2Name <- paste(c("StDev for h= ", toString(h)), collapse="")

Col3Name <- paste(c("MAE for h= ", toString(h)), collapse="")

colnames(Stat.matrix) <- c("Sample Size (n)", Col2Name, Col3Name, "ErrorMean", "ErrorMin",

"ErrorMax")

#Set up Intcal13 calibration curve

Lab\_Error <- StandardRadError

eps = 1e-05

pathToCalCurves = system.file("data", package = "Bchron")

calCurveFile <- paste(pathToCalCurves, "/", "intcal13", ".txt.gz", sep = "")

calCurve = calBP = c14BP = calSd = ageGrid = list()

calCurve <- as.matrix(read.table(calCurveFile))

#Calendar years for plotting calibration curve, x values

calBP <- calCurve[, 1]

#Radiocarbon years for plotting calibration curve, y values

c14BP <- calCurve[, 2]

#Error for calendar ages

calSd <- calCurve[, 3]

#Create an age grid that runs from through all radiocarbon years in increments of 1

ageGrid <- seq(min(c14BP), max(c14BP), by = 1)

#Linear interpolation of calibration curve

Intcal13 <- approx(c14BP, calBP, xout = ageGrid)$y

Intcal13Sd <- approx(c14BP, calSd, xout = ageGrid)$y

RadVsCal <- data.frame(RCYBP = ageGrid, CalBP=Intcal13)

#Error

tau <- sqrt(Lab\_Error^2 + Intcal13Sd)

#BEGIN ANALYSIS

#Cycle through sample size (from 1 to g)

for(n in seq(from=1, to=g, by=j)) {

#Cycle through error stat calculations for sample size = {1, 2, 3, .., g}

for(p in RepVec) {

#Update the user on the progress of runs

Update <- paste(c("For sample size ", toString(n), " out of ", toString(g),

" iteration ", toString(p), " out of ", toString(h), ": "),

collapse = "")

print(Update, quote = FALSE)

#Sample atlatl calendar dates (CYBP)

AtlSample <- sample(AtlRange, size = n, replace = FALSE, prob = NULL)

#prob = vector input changing prob of selecting each yr. Could be used to correct for taphonomy.

#Sample bow calendar dates (CYBP)

BowSample <- sample(BowRange, size = n, replace = FALSE, prob = NULL)

#REVERSE CALIBRATE Samples

#Atlatl Samples

#Create an empty vector to store all R\_Simulate dates

R\_SimsAtl <- rep(NA, length(AtlSample))

iterator <- 0

for(s in AtlSample) {

iterator <- iterator + 1

#Calculate density distribution function for the t distribution with degrees of freedom

dens <- dt((s - Intcal13)/tau, df = 100)

dens <- dens/sum(dens)

#Output:

#ageGrid = probable RCYBP ages for given R\_Simulate date

#densities = probability density at each position

out = list(R\_simulate = s, Lab\_Error = Lab\_Error,

calCurves = "Intcal13", ageGrid = ageGrid[dens > eps], densities = dens[dens > eps])

names(out) = c("R\_Simulate ", "Lab Error", "Cal Curve", "RCYBP", "Relative Probability")

class(out) = "BchronCalibratedDates"

RCYBP\_Sim <- sample(out$RCYBP, 1, prob = out$"Relative Probability")

R\_SimsAtl[iterator] <- RCYBP\_Sim

}

AtlAges <- R\_SimsAtl

#Bow Samples

#Create an empty vector to store all R\_Simulate dates

R\_SimsBow <- rep(NA, length(BowSample))

iterator <- 0

for(s in BowSample) {

iterator <- iterator + 1

#Calculate density distribution function for the t distribution with degrees of freedom

dens <- dt((s - Intcal13)/tau, df = 100)

dens <- dens/sum(dens)

#Output:

#ageGrid = probable RCYBP ages for given R\_Simulate date

#densities = probability density at each position

out = list(R\_simulate = s, Lab\_Error = Lab\_Error,

calCurves = "Intcal13", ageGrid = ageGrid[dens > eps], densities = dens[dens > eps])

names(out) = c("R\_Simulate ", "Lab Error", "Cal Curve", "RCYBP", "Relative Probability")

class(out) = "BchronCalibratedDates"

RCYBP\_Sim <- sample(out$RCYBP, 1, prob = out$"Relative Probability")

R\_SimsBow[iterator] <- RCYBP\_Sim

}

BowAges <- R\_SimsBow

#Re-Calibrate Dates

#Vectors of radiocarbon standard error

AtlSds <- mat.or.vec(n, 1)

AtlSds[1:n] <- StandardRadError

BowSds <- mat.or.vec(n, 1)

BowSds[1:n] <- StandardRadError

#Vector indicating calibration curve

calCurves <- toString(mat.or.vec(n, 1))

calCurves[1:n] <- "intcal13"

#Re-calibrate the dates

AtlCalib <- BchronCalibrate(ages=AtlAges, ageSds=AtlSds, calCurves=calCurves)

BowCalib <- BchronCalibrate(ages=BowAges, ageSds=BowSds, calCurves=calCurves)

#Determine range of summed probability distribution

#Create a vector of names of AtlDens$calAges$daten$ageGrid

ageGridNamesAtl <- toString(mat.or.vec(n,1))

for (i in seq.int(from=1, to=n)) {

dateNum <- i

dateNumStr <- toString(dateNum)

dateNumTitle <- paste(c("AtlCalib$date", dateNumStr, "$ageGrid"), collapse="")

ageGridNamesAtl[dateNum] <- dateNumTitle

}

SumAtlDates <- rep(NA, 1)

for (i in seq.int(from=1, to=n)){

CurrentIteration <- eval(parse(text=ageGridNamesAtl[i]))

SumAtlDates <- append(CurrentIteration, SumAtlDates)

}

#Create a vector of name of BowDens$calAges$daten$ageGrid

ageGridNamesBow <- toString(mat.or.vec(n,1))

for (i in seq.int(from=1, to=n)) {

dateNum <- i

dateNumStr <- toString(dateNum)

dateNumTitle <- paste(c("BowCalib$date", dateNumStr, "$ageGrid"), collapse="")

ageGridNamesBow[dateNum] <- dateNumTitle

}

SumBowDates <- rep(NA, 1)

for (i in seq.int(from=1, to=n)){

CurrentIteration <- eval(parse(text=ageGridNamesBow[i]))

SumBowDates <- append(CurrentIteration, SumBowDates)

}

#Find the min and max of all age values to give range of summed p distribution

SumAtlRange <- range(SumAtlDates, na.rm=TRUE)

SumAtlRangeString <- toString(SumAtlRange)

print(c("Re-Calibrated Atlatl Date Range (CYBP): ", SumAtlRangeString), quote = FALSE)

SumBowRange <- range(SumBowDates, na.rm=TRUE)

SumBowRangeString<- toString(SumBowRange)

print(c("Re-Calibrated Bow Date Range (CYBP): ", SumBowRangeString), quote = FALSE)

#Calculate overlap/separation of summed probability distributions

Overlap <- SumBowRange[2] - SumAtlRange[1]

CurrentResult <- paste(c("Error: ", toString(Overlap), " calendar years"), collapse = "")

print(CurrentResult, quote = FALSE)

#Store overlap/separation for this n, repeat h times for this n

Overlap.h.Iterations[p] <- Overlap

}

#Calculate error measurements of overlap/separation for this n

SDforNreps <- sd(Overlap.h.Iterations, na.rm = TRUE)

MeanForNreps <- mean(Overlap.h.Iterations, trim = 0, na.rm = TRUE)

MinForNreps <- min(Overlap.h.Iterations, na.rm = TRUE)

MaxForNreps <- max(Overlap.h.Iterations, na.rm = TRUE)

AbsOverhIt <- abs(Overlap.h.Iterations)

MAEforNreps <- mean(AbsOverhIt, trim = 0, na.rm = TRUE)

Stat.matrix[n/j, 1] <- n

Stat.matrix[n/j, 2] <- SDforNreps

Stat.matrix[n/j, 3] <- MAEforNreps

Stat.matrix[n/j, 4] <- MeanForNreps

Stat.matrix[n/j, 5] <- MinForNreps

Stat.matrix[n/j, 6] <- MaxForNreps

Overlap.h.Iterations <- rep(NA, h)

write.csv(Stat.matrix, file = "StatMatrix.csv", na="")

}

print(head(Stat.matrix))

print("...")

print(tail(Stat.matrix))