## SUPPLEMENTARY MATERIALS

## **Participant Enrollment**

One hundred and ninety-five participants were enrolled of whom 132 completed the study. Thirtyseven participants were excluded because exclusion criteria were detected during the clinical interview. Twenty-one participants withdrew consent: Nineteen participants left the study due to scheduling conflicts, 1 participant met exclusion criteria while undergoing the study, and 1 dropped out due to medical issues unrelated to the study. Finally, the participation of 5 subjects was terminated by the investigators, because they could not tolerate the MRI environment (n = 4) and polysomnography (n = 1). Participants were compensated \$500 if they completed the study.



Figure S1. Distribution of CAPS-5 score in the sample.



**Figure S2.** Timeline of the study procedures. The sleep data analyzed in this study was obtained during the consolidation night.



**Figure S3.** Partial regression (added variable) plots of the significant REM variables in the regression analyses that tested the hypothesis 1 for physiological extinction recall (ERI). The Y axis represents the residuals derived from regressing ERI on all the predictor variables in the corresponding model, except the variable noted on the X axis. The X axis represents the residuals derived from regressing the predictor variable noted on the X axis on all the other predictor variables in the corresponding models. The slope reflects the standardized partial regression coefficient ( $\beta$ ). Note that smaller ERI denotes better physiological extinction recall. HF[ms<sup>2</sup>]: Absolute power of high frequency heart rate variability; %REM: Proportion of REM sleep to total sleep time; REMD: REM density; REML: REM latency.



**Figure S4.** Partial regression (added variable) plots of the significant REM variables in the regression analyses that tested the hypothesis 1 (A), and the hypothesis 2 (B), for subjective extinction recall (sERI). The Y axis represents the residuals derived from regressing sERI on all the predictor variables in the corresponding model, except the variable noted on the X axis. The X axis represents the residuals derived from regressing the predictor variables in the corresponding model. The slope reflects the standardized partial regression coefficient ( $\beta$ ). Note that smaller sERI denotes better subjective extinction recall. HF[ms<sup>2</sup>]: Absolute power of high frequency heart rate variability; REMD: REM density.

Model	Predictors	В	SE	β	t	р	95%	∕₀ CI					
1	Sex	603	.351	242	-1.714	.092	-1.307	.102					
	Medication	075	.396	025	189	.850	869	.719					
	%REM	052	.026	281	-2.004	.050	104	.000					
	REMD	.147	.053	.391	2.793	.007	.041	.253					
	REML	010	.004	383	-2.688	.010	017	003					
	REMF	.034	.032	.148	1.035	.305	032	.099					
									Char	nge		AN	OVA
									ΔF	р	Adj. R <sup>2</sup>	F	р
2	Sex	651	.345	261	-1.886	.065	-1.344	.042	2.553	.088	.162	2.450	.025
	Medication	.064	.396	.022	.162	.872	730	.859					
	%REM	058	.026	313	-2.280	.027	109	007					
	REMD	.159	.053	.423	3.030	.004	.054	.265					
	REML	012	.004	446	-3.122	.003	019	004					
	REMF	.028	.032	.124	.885	.380	036	.092					
	HF[ms <sup>2</sup> ]	401	.201	345	-1.999	.051	803	.002					
	HF[ms <sup>2</sup> ]×Sex	.635	.294	.391	2.160	.035	.045	1.224					

**Table S1.** Hierarchical regression analysis for physiological extinction recall (ERI) with all REM variables included in the model. Note that smaller ERI denotes better extinction recall. HF[ms<sup>2</sup>]: Absolute power of high frequency heart rate variability; %REM: Proportion of REM sleep to total sleep time; REMD: REM density; REMF: REM fragmentation; REML: REM latency.

Model	Predictors	B	SE	β	t	р	95%	6 CI					
1	Age	265	.655	045	404	.687	-1.569	1.039					
	Sex	.029	7.341	.000	.004	.997	-14.589	14.646					
	Medication	-17.151	8.405	232	-2.041	.045	-33.886	415					
	%REM	.246	.543	.055	.453	.652	836	1.328					
	REMD	2.663	.993	.317	2.681	.009	.685	4.640					
	REML	.066	.078	.103	.847	.400	090	.222					
	REMF	.823	.671	.145	1.227	.224	513	2.159					
									Chai	nge		AN	OVA
									ΔF	р	Adj. R <sup>2</sup>	F	р
2	Age	433	.640	073	676	.501	-1.707	.842					
	Sex	1.142	7.143	.018	.160	.873	-13.083	15.368	5.681	.020	.137	2.671	.012
	Medication	-20.916	8.312	283	-2.516	.014	-37.471	-4.362					
	%REM	.217	.528	.048	.411	.682	834	1.268					
	REMD	2.399	.971	.286	2.472	.016	.466	4.332					
	REML	.067	.076	.103	.877	.383	085	.218					
	REMF	.800	.651	.141	1.228	.223	498	2.097					

**Table S2.** Hierarchical regression analysis for subjective extinction recall (sERI) with all REM variables included in the model. Note that smaller sERI denotes better extinction recall. HF[ms<sup>2</sup>]: Absolute power of high frequency heart rate variability; %REM: Proportion of REM sleep to total sleep time; REMD: REM density; REMF: REM fragmentation; REML: REM latency.

Model	Predictors	В	SE	β	t	р	95%	CI					
1	Sex	531	.345	213	-1.539	.130	-1.221	.160					
	Medication	.017	.386	.006	.045	.964	757	.791					
	%REM	043	.025	234	-1.763	.083	093	.006					
	REMD	.143	.053	.379	2.718	.009	.037	.248					
	REML	008	.003	323	-2.481	.016	015	002					
									Cha	nge		AN	OVA
									ΔF	р	Adj. R <sup>2</sup>	F	р
2	Sex	581	.337	233	-1.726	.090	-1.256	.094	2.700	0.076	0.164	2.686	0.019
	Medication	.088	.382	.030	.231	.818	679	.855					
	%REM	049	.024	266	-2.051	.045	098	001					
	REMD	.151	.052	.402	2.914	.005	.047	.256					
	REML	010	.003	390	-2.981	.004	017	003					
	RMSSD	872	.396	375	-2.200	.032	-1.667	077					
	RMSSD×Sex	1.209	.580	.369	2.085	.042	.046	2.371					

**Table S3.** Hierarchical regression analysis for physiological extinction recall (ERI). RMSSD and RMSSD  $\times$  Sex interaction were significant predictors. Note that smaller ERI denotes better extinction recall. %REM: Proportion of REM sleep to total sleep time; REMD: REM density; REML: REM latency; RMSSD: Root mean square of successive differences.

Model	Predictors	В	SE	β	t	р	95%	- CI					
1	Age	506	.630	085	803	.424	-1.761	.748					
	Sex	224	7.153	004	031	.975	-14.458	14.010					
	Medication	-14.982	8.278	203	-1.810	.074	-31.456	1.492					
	REMD	2.917	.970	.348	3.006	.004	.986	4.849					
									Cha	nge		ANO	VA
									ΔF	р	Adj. R <sup>2</sup>	F	р
2	Age	628	.620	106	-1.013	.314	-1.861	.605	4.515	0.037	0.133	3.265	0.010
	Sex	.062	7.002	.001	.009	.993	-13.875	13.999					
	Medication	-18.339	8.255	248	-2.222	.029	-34.770	-1.909					
	REMD	2.758	.953	.329	2.895	.005	.862	4.655					
	RMSSD	-12.436	5.853	225	-2.125	.037	-24.085	787					

**Table S4.** Hierarchical regression analysis for subjective extinction recall (sERI). Addition of RMSSD significantly increased the proportion of variance explained by the model. Note that smaller sERI denotes better extinction recall. REMD: REM density; RMSSD: Root mean square of successive differences.

									ANO	VA
Predictors	В	SE	β	t	р	95%	6 CI	Adj. R <sup>2</sup>	F	р
Sex	604	.325	236	-1.856	.068	-1.255	.046	.141	3.702	.009
%REM	050	.023	271	-2.190	.032	096	004			
REMD	.139	.051	.362	2.755	.008	.038	.241			
REML	009	.003	359	-2.933	.005	016	003			

**Table S5.** Linear regression analysis for physiological extinction recall (ERI). Noncontributory predictors included in the original model (see the manuscript) are removed. Note that smaller ERI denotes better extinction recall. %REM: Proportion of REM sleep to the total sleep time; REMD: REM density; REML: REM latency.

									ANO	VA
Predictors	В	SE	β	t	р	95%	6 CI	Adj. R <sup>2</sup>	F	р
REMD	2.363	.876	.268	2.698	.008	.624	4.103	.062	7.277	.008

**Table S6.** Linear regression analysis for subjective extinction recall (sERI). Non-contributory predictors included in the original model (see the manuscript) are removed. Note that smaller sERI denotes better extinction recall. REMD: REM density.

									ANO	VA
Predictors	В	SE	β	t	р	95%	ó CI	Adj. R <sup>2</sup>	F	р
Sex	559	.324	224	-1.726	.090	-1.208	.090	.179	3.177	.010
%REM	.158	.052	.420	3.063	.003	.055	.261			
REMD	051	.024	273	-2.115	.039	099	003			
REML	010	.003	392	-3.024	.004	017	003			
HF[ms <sup>2</sup> ]	413	.198	356	-2.092	.041	809	017			
HF[ms <sup>2</sup> ]×Sex	.630	.285	.389	2.211	.031	.059	1.202			

**Table S7.** Final model in the hierarchical regression analysis for physiological extinction recall (ERI), after non-contributory predictors included in the original model (see the manuscript) are removed. Note that smaller ERI denotes better extinction recall. %REM: Proportion of REM sleep to the total sleep time; HF[ms<sup>2</sup>]: Absolute power of high frequency heart rate variability; REMD: REM density; REML: REM latency.

									ANO	VA
Predictors	В	SE	β	t	р	95%	CI	Adj. R <sup>2</sup>	F	р
Medications	-17.781	8.015	241	-2.218	.029	-33.727	-1.834	.140	5.568	.002
REMD	2.722	.902	.324	3.019	.003	.928	4.516			
HF[ms <sup>2</sup> ]	-6.619	2.877	240	-2.301	.024	-12.343	895			

**Table S8.** Final model in the hierarchical regression analysis for subjective extinction recall (sERI), after non-contributory predictors included in the original model (see the manuscript) are removed. Note that smaller sERI denotes better extinction recall. %REM: Proportion of REM sleep to the total sleep time; HF[ms<sup>2</sup>]: Absolute power of high frequency heart rate variability; REMD: REM density.

## **Reliability of Heart Rate Variability Measures Across Baseline and Consolidation Nights**

To examine the stability of vagally mediated heart rate variability across baseline and consolidation nights, we calculated the intraclass correlation coefficients (ICC) for both HF[ms<sup>2</sup>] and RMSSD. Heart rate variability indexes from the baseline night was reported in a previous study (Daffre et al. 2023), which calculated the HRV metrics differently from the current study. In the previous study, time-weighted averages (in contrast to the simple averages in the current study) were used for all indexes, and frequency domain metrics were calculated using Fourier transformation (in contrast to the autoregressive method used in the current study). Despite these methodological differences, both indexes showed high reliability across the two nights:

	ICC	95% Confidence Interval					
HF-HRV	0.92	.864	.948				
RMSSD	0.90	.835	.936				

\*HF-HRV: High-frequency heart rate variability; ICC: Intraclass correlation coefficient.

## Association of Heart Rate Variability With Demographic and Clinical Variables

 $HF[ms^2]$  was not associated with age (F(1,89)=1.137, p=0.289), sex (F(1,89)=0.199, p=0.656), PTSD diagnosis (F(1,89)=.264, p=0.608), depressive symptom severity as measured by Quick Inventory of Depressive Symptomatology (QIDS; F(1,89)=0.795, p=0.375) or the severity of posttraumatic stress symptoms as measured by Clinician-Administered PTSD Scale for DSM-5 (CAPS-5; F(1,89)=0.444, p=0.507). Medication use (benzodiazepines or antidepressants) was associated with lower HF[ms<sup>2</sup>] (F(1,89)=5.123, p=0.026).

Daffre C, Oliver KI, Nazareno JRS, Mader T, Seo J, Dominguez JP, Gannon K, Lasko NB, Orr SP and Pace-Schott EF (2023) Rapid eye movement sleep parasympathetic activity predicts wake hyperarousal symptoms following a traumatic event. J Sleep Res 32(1), e13685. <u>https://doi.org/10.1111/jsr.13685</u>.